

Robust Fractional Order Gain-Scheduled Control Design for LPV Systems using an Adaptive Switching Law

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ABSTRACT

This paper presents a robust adaptive control structure design based on gain scheduled control. The proposed control configuration uses a set of switching predefined PID controllers to deal with fractional order linear parameter varying (LPV) systems. The switching law is based only on the models' outputs. A class of fractional second-order like systems is considered. Simulation example results and discussion illustrate the efficiency of the proposed method.

Keywords: LPV system, Gain scheduled control, Fractional order system

1 Introduction

Recently, fractional order systems have had a great impact on the engineering research community. The main motivation is their ability to improve both the performance and the robustness of the resulting models, especially in the control domain [1]- [3].

The main objective of this research is to propose a generalization of the robust gain scheduled linear parameter varying (LPV) PID controller [4], [5] to a class of fractional second-order LPV systems, considering robust stability, performances, closed-loop pole constraints and particularly the time varying nature of the plant. The measurement (estimation) of the varying parameter is obtained in real-time and used to adjust PID parameters.

The LPV PID controller design should be considered as an output feedback control that is usually used with LMI's to solve a non-convex optimization problem [6], [7]. However, in regard of the special configuration of the considered plant model (second order), the idea here is to tune the PID controllers and reformulate it as a convex state-feedback problem. After that, a coupled two-tanks second order system will be subject of the proposed LPV-based control approach.

2 LPV control problem statement

$$G_{LPV_{ref}}(s) = \frac{1.1081\varphi_1}{s^2 + 0.5085(\varphi_1 + \varphi_2)s + 0.2585\varphi_1\varphi_2} \quad (1)$$

$$G_\varphi(s) = \frac{1.1081\varphi_1}{(s^2 + 0.5085(\varphi_1 + \varphi_2)s + 0.2585\varphi_1\varphi_2)^\mu} \quad (2)$$

Where μ is a real number such that $0 < \mu < 1$. They are approximated by low order transfer functions using the singularity method of Charef [6]. Given the LPV system in Eq. (1) or the fractional order LPV system (2), find a gain scheduling PID controller that guarantees the stability and the high performances of 2nd order integer and fractional system.

3 Simulation example and discussion

A coupled two-tanks is the case study illustrating the proposed LPV PID design scheme. A coupled two-tanks is the case study illustrating the proposed LPV PID design scheme. In order to obtain the fractional model, we approximate the system represented in (2) by a 4th or 5th order transfer function using the



singularity method [6] and then the gains scheduling approach is applied to this system. The fractional order μ is chosen equal to: $\mu = 0,6$. by computing the LPV PID controller gains with PID Toolbox in MATLAB, we obtain the closed-loop responses shown in Figure 1.

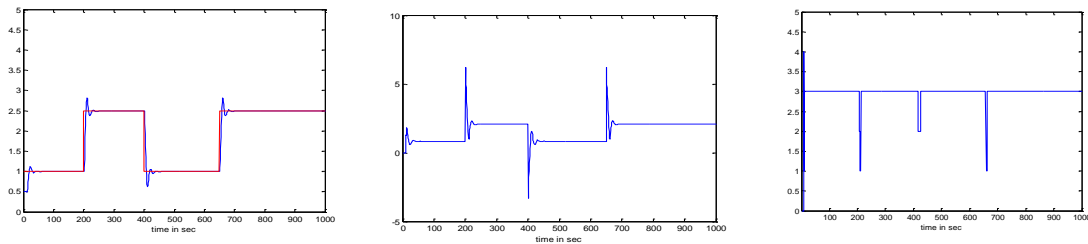


Figure 1: Fractional order system response: (a) Output signal (b) Control signal (c) Switching index

A very important advantage of the proposed fractional order model based controller is the elimination of the chattering phenomena and the high values of the control signals.

4 Conclusion

The main contribution of this paper is to propose an innovative approach to design a gain-scheduled PID for fractional order LPV systems, using an improved switching law based on the plant output. The fractional PID controller design can be viewed as a state-feedback controller. This approach has successfully been applied to a real case study based on the control of a two coupled-tanks with satisfactory performance results giving supplementary benefits: chattering elimination and lowering the amplitude of the control signals.

5 Competing Interests

The authors declared that no conflict of interest exists in this work.

How to Cite

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